# Low-Cot Seff-Tet of OryptoDevices 

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## Motivation

- Secure circuits testing
$\checkmark$ Scan path
- High fault coverage
- Automatic generation of scan chains
- Easy test sequence generation


## $\checkmark$ Vulnerability

- Control and observation of internal states of CUT
- => secret data retrieval

Scan based attack DES [Yan et al., ITC 04]
AES [Yan et al., IEEE TCAD 06]
BIST

## Motivation

## - BIST

$\checkmark$ Reduced ATE cost
$\checkmark$ In-situ testing
$\checkmark$ Reduced external access
-But
$\checkmark$ Circuitry overhead

- test controller
- pattern generator
- signature analyzer...


## Motivation

- Secure circuits contain a crypto core
- E.g. Smart cards

- Crypto core => Test resource


## Outline

## AES \& DES

$\checkmark$ Algorithm \& architecture
$\checkmark$ Testability issues

- AES/DES as pattern generators
- AES/DES Self test

Optimisations
Conclusion

## Introduction

- Symetric cryptography


DES
$\checkmark$ Adopted as standard in 1976
$\checkmark$ Data : 64 bits, Key : 56 bits

- AES : Advanced Encryption Standard
$\checkmark$ Adopted as standard in 2001
$\checkmark$ Data: 128 bits, Key: 128 bits $(192,256)$
" Crypto algorithms basis: Diffusion \& Confusion


## Characteristics

- Diffusion and confusion
$\checkmark$ Confusion refers to making the relationship between the key and the ciphertext as complex and involved as possible.
$\checkmark$ Diffusion refers to the property that redundancy in the statistics of the plaintext is "dissipated" in the statistics of the ciphertext. For diffusion to occur a change in a single bit of the plaintext should result in changing the value of many ciphertext bits.
- Iterative algorithms (rounds)

Each round is a "bijective" operation

## DES algorithm \& architecture



## AES Algorithm \& architecture



## Cyphering \& testability

- Diffusion
$\checkmark$ every input bit of a round influences many output bits, i.e. every input line of a round is in the logic cone of many output bits.
$\checkmark$ an error caused by a fault in the body of the round is very likely to propagate to the output.
$\checkmark$ observability
- Bijective
$\checkmark$ controllability
- Highly testable hardware implementations
$\checkmark$ => random testing


## AES/DES as test pattern generator

One test pattern = Intermediate round result of encryption


Test pattern

## AES/DES as TPG: randomness analysis

NIST Special Publication 80022
[NIST 800-22]


Statistical package of 15 tests has been developed to test binary sequences randomness

| $1:$ Monobit Test |
| :--- |
| $2:$ Block Frequency Test |
| $3:$ Cumulative Sums Forward (Reverse) |
| $4:$ Runs Test |
| $5:$ Long Runs of Ones Test |
| $6:$ Rank Test |
| 7 : Discrete Fourier Transform (Spectral) Test |
| $8:$ Universal Statistical Test |
| $9:$ Approximate Entropy Test |
| $10:$ Serial Test |
| $11:$ Linear Complexity Test |
| $12:$ Aperiodic Templates |
| $13:$ Periodic Template Test |
| $14:$ Random Excursion Test |
| $15:$ Random Excursion Variant Test |

## 1-round AES/DES : randomness

1.5 Mbit bitstream (leftmost bit)

Test passes if $x>0.1$

| $\mathrm{X}>0.1$ | 1_round <br> AES | 1_round <br> DES | LFSR |
| :--- | :---: | :---: | :---: |
| Frequency | 0.71209 | 0.45847 | 0.00256 |
| Blk-freq | 0.47556 | 0.87065 | 0.44150 |
| Runs | 0.64156 | 0.18337 | 0.14362 |
| Long Runs | 0.28546 | 0.15829 | 0.96593 |
| Rank | 0.35722 | 0.24411 | 0.52660 |
| DFT | 0.03397 | 0.61040 | 0.81051 |
| Aperiodic | 0.50704 | 0.50541 | 0.49963 |
| Periodic | 0.08345 | 0.90055 | 0.39384 |
| Univ.Maurer | 0.44635 | 0.86625 | 0.24403 |
| Lincomp | 0.86761 | 0.88996 | 0 |
| Serial | 0.62350 | 0.42735 | 0.71383 |
| Apen | 0.44173 | 0.41358 | 0.63747 |
| Cusum | 0.73566 | 0.55751 | 0.00326 |
| Random | 0.41284 | 0.36790 | 0 |
| Variant-R | 0.49847 | 0.24177 | 0 |

## 1-round AES/DES : randomness

Proportion of bitstreams passing each NIST test


LFSR


randomness:
"1-round AES" $\approx$ " 1 -round DES" $\approx$ LFSR

## AES Self-test

Cycle 1


## AES Self-test



When?

## AES Self-test



## AES Self-test



## AES Self-test



## AES Self-test

- How many random patterns are needed to get those 203 deterministic patterns? "The Coupon Collector Problem"

$$
\begin{aligned}
\mathrm{P}\left(\mathrm{X}_{1} \cap \mathrm{X}_{2} \cap \ldots \cap \mathrm{X}_{\mathrm{k}}\right)=1-\sum_{\mathrm{j}=1}^{\mathrm{k}}(-1)^{\mathrm{j}-1} \mathrm{C}_{\mathrm{k}}^{\mathrm{j}}\left(\frac{\mathrm{~m}-\mathrm{j}}{\mathrm{~m}}\right)^{\mathrm{T}} \\
\mathrm{~m}=2^{128}
\end{aligned}
$$

Sbox implementation:
$\checkmark$ \#test vectors $\in\{200, \ldots, 256\}=>T \in\{2520, \ldots, 2590\}$

## AES Self-test

## " "Pseudo" Fault Simulation

Result :

$\checkmark$ Fault coverage: 100\% after 2534 cycles
$\checkmark$ Test time reduction: 2400 cycles (with several keys, several plaintexts)

- Specific plaintext, specific key for minimal test time?


## DES Self-test

Right bits


## DES Self-test

Right bits


## DES random sequence length

$$
\begin{aligned}
& P\left(X_{1} \cap X_{2} \cap \ldots \cap X_{k}\right)=1-\sum_{j=1}^{k}{ }_{(-1)}{ }^{j-1} c_{k}^{j}\left(\frac{m-j}{m}\right)^{T} \\
& \mathrm{~m}=2^{64} \quad \mathrm{k}=\# \text { vectors }=64 \\
& \mathrm{P}\left(\mathrm{X}_{1} \cap \mathrm{X}_{2} \cap \ldots \cap \mathrm{X}_{\mathrm{k}}\right)=99 \% \quad \Longrightarrow T=540 \\
& \text { random patterns (540 rounds) } \\
& 34 \text { encryptions }
\end{aligned}
$$

Results : 100\% FC after 24 encryptions (Data path and control)

## Optimisation

## Speeding up self-test of AES

$\checkmark 2500$ cycles for 256 test patterns
$\checkmark$ Feed-back on Sbox


5 cycles in state graph =>

| Length | States |
| :---: | :---: |
| 59 | 63,FB,F,76,38,7,C5,A6,24,36,5,6B,7F,D2,B5,D5, 3,7B, 21, FD, $54,20, B 7, A 9, D 3,66,33, C 3,2 \mathrm{E}, 31, \mathrm{C} 7$, C6,B4,8D,5D,4C, $29, A 5,6,6 F, A 8, C 2,25,3 F, 75,9 D$, 5E,58,6A,2,77,F5,E6,8E,19,D4,48,52,0 |
| 81 | 7C,10,CA,74,92,4F,84,5F,CF,8A,7E,F3,D,D7,E,AB, 62,AA,AC,91,81,C,FE,BB,EA, 87,17,F0,8C,64,43,1A, A2,3A, 80, CD, BD, 7A, DA, $57,5 B, 39,12, C 9, D D, C 1,78$, BC,65,4D,E3,11,82,13,7D,FF,16,47,A0,E0,E1,F8,41, 83,EC,CE,8B,3D,27,CC,4B,B3,6D,3C,EB,E9,1E,72,40,9,1 |
| 87 | F2,89,A7,5C,4A,D6,F6,42,2C,71,A3,A,67,85,97,88, C4,1C,9C,DE,1D,A4,49,3B,E2,98,46,5A,BE,AE,E4, 69,F9,99,EE,28,34,18,AD,95,2A,E5,D9,35,96,90,60,D0, 70,51,D1,3E,B2,37,9A,B8,6C,50,53,ED,55,FC,B0,E7, $94,22,93, D C, 86,44,1 B, A F, 79, B 6,4 E, 2 F, 15,59, C B, 1 F$, C0,BA,F4,BF, 8,30,4 |
| 27 | 2B,F1,A1,32, 23, 26, F7, 68, 45,6E,9F,DB,B9,56,B1,C8, E8,9B,14,FA,2D,D8,61,EF,DF,9E, B |
| 2 | 8F,73 |

- Add a (simple) feed-back function for traversing all 256 states $g=\operatorname{exor}(01110110) \rightarrow 5$ inverters



## Optimisation

- 2 steps procedure
$\checkmark$ test of Sboxes: 256 cycles (vs 2400)
$\checkmark$ test of remaining logic: 16 cycles
- Area overhead : 1\%


Register / MISR

## Conclusion

## - AES/DES as TPG

$\checkmark$ Randomness: better than LFSRs

- Self Testability
$\checkmark$ AES: 2400 encryption rounds (of a single message)
$\checkmark$ DES: 540 encryption rounds (of a single message)
$\checkmark$ Suitable technique for other ciphering circuits (IDEA, Fox, Blowfish, ...)
$\checkmark$ No area overhead
$\checkmark$ No impact on performance
$\checkmark$ No impact on security



## References

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- [Yan04]: B. Yang, K. Wu, R. Karri, Polytechnic University, "Scan-based Side-Channel Attack on Dedicated Hardware Implementations on Data Encryption Standard", International Test Conference (ITC 2004), Charlottes, USA, October 26-28, pp 339-344
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" [ [Yan, FDTC 05]: B. Yang \& R. Karri, "Crypto BIST: A Built-In Self Test Architecture for Crypto Chips", 2nd Workshop on fault diagnosis and tolerance in cryptography (FDTC 2005), pp 95-108
- [NIST 800-22]: A statistical test suite for random and pseudorandom number generators for cryptographic applications NIST Special Publication 800-22 (with revisions dated May 15, 2001)


## Statistical tests NIST

- -Monobit Test: determine whether the number of ones and zeros in a sequence are approximately the same as would be expected for a truly random sequence.
- Block Frequency Test: determine whether the number of ones and zeros in each of $M$ non-overlapping blocks created from a sequence appear to have a random distribution.
-     - Cumulative Sums Forward (Reverse) Test: determine whether the sum of the partial sequences occurring in the tested sequence is too large or too small.
-     - Runs Test: determine whether the number of runs of ones and zeros of various lengths is as expected for a random sequence. In particular, this test determines whether the oscillation between such substrings is too fast or too slow.
-     - Long Runs of Ones Test: determine whether the longest run of ones within the tested sequence is consistent with the longest run of ones that would be expected in a random sequence.
-     - Rank Test: check for linear dependence among fixed length substrings of the original sequence.
-     - Discrete Fourier Transform (Spectral) Test: detect periodic features (i.e., repetitive patterns that are near each other) in the tested sequence that would indicate a deviation from the assumption of randomness.
-     - Aperiodic Templates Test: reject sequences that exhibit too many occurrences of a given non-periodic (aperiodic) pattern.
-     - Periodic Template Test: reject sequences that show deviations from the expected number of runs of ones of a given length.
-     - Universal Statistical Test: detect whether or not the sequence can be significantly compressed without loss of information. A compressible sequence is considered to be nonrandom.
-     - Approximate Entropy Test: compare the frequency of overlapping blocks of two consecutive/adjacent lengths ( $m$ and $m+1$ ) against the expected result for a normally distributed sequence.
-     - Random Excursion Test: determine if the number of visits to a state within a random walk exceeds what one would expect for a random sequence.
-     - Random Excursion Variant Test: detect deviations from the distribution of the number of visits of a random walk to a certain state.
-     - Serial Test: determine whether the number of occurrences of m-bit overlapping patterns is approximately the same as would be expected for a random sequence.
-     - Linear Complexity Test: determine whether or not the sequence is complex enough to be considered random.

