

A Modelling Framework for Quantitative Analysis of Interdependencies in Electrical Power Systems

in the context of the EU CRUTIAL project

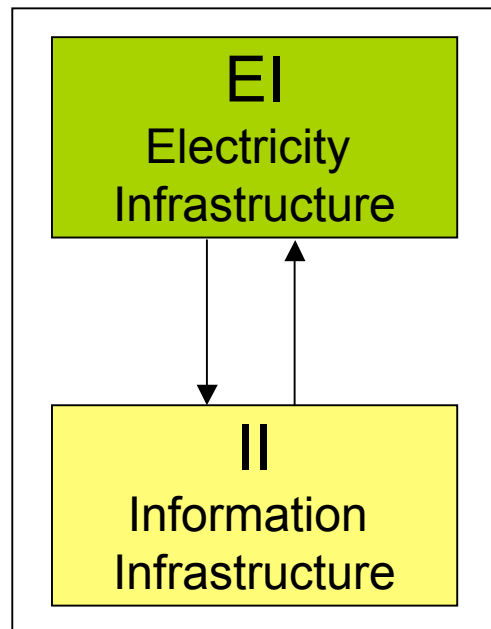
Felicita Di Giandomenico
CNR-ISTI

Joint work with Silvano Chiaradonna and Paolo Lollini

Objective

- Define a conceptual **modeling framework** well suited to characterize and analyze the **interdependencies** between
 - the information infrastructure
 - the controlled power infrastructure
- The focus is on **interdependence-related failure**:
 - Cascading failures
 - Escalating failures
 - Common-cause failures
- The goal is to **quantitatively assess** their impact on the resilience of these infrastructures
- The aim is to have a **general evaluation framework**, populated by building blocks, representing basic events, and composable to potentially represent any EPS configurations

Hierarchical modeling framework for the quantitative evaluation of interdependencies



- Capture structural and behavioral aspects of EI and II components
- Major modelling framework characteristics:
 - Hierarchical composition using reusable generic submodels
 - Different formalisms for different submodels
 - Discrete and hybrid state representation
 - Performability measures for quantifying the impact of interdependencies
 - Combination of analytical and simulation solution techniques

Feasibility studies

Two directions:

- Investigation of the framework's feasibility using the multi-formalism, multi-solution tool Möbius and SAN formalism
- Development of an ad-hoc simulator, as a useful support to better understand specific phenomena

Investigation of the framework's feasibility using Möbius and SAN

The basic modeling mechanisms have been implemented using **Stochastic Activity Networks** and **Möbius** tool, focusing on:

- **Electrical Infrastructure components:**
 - **Nodes** (Substations, Generators and Loads)
 - **Power Lines**
 - **Protections**
- **Information Infrastructure components:**
 - **Local operations $RS_1()$** (performed by LCS), and
 - **Global operations $RS_2()$** (performed by RTS)
 - **TSOcomNetw:** public or private network

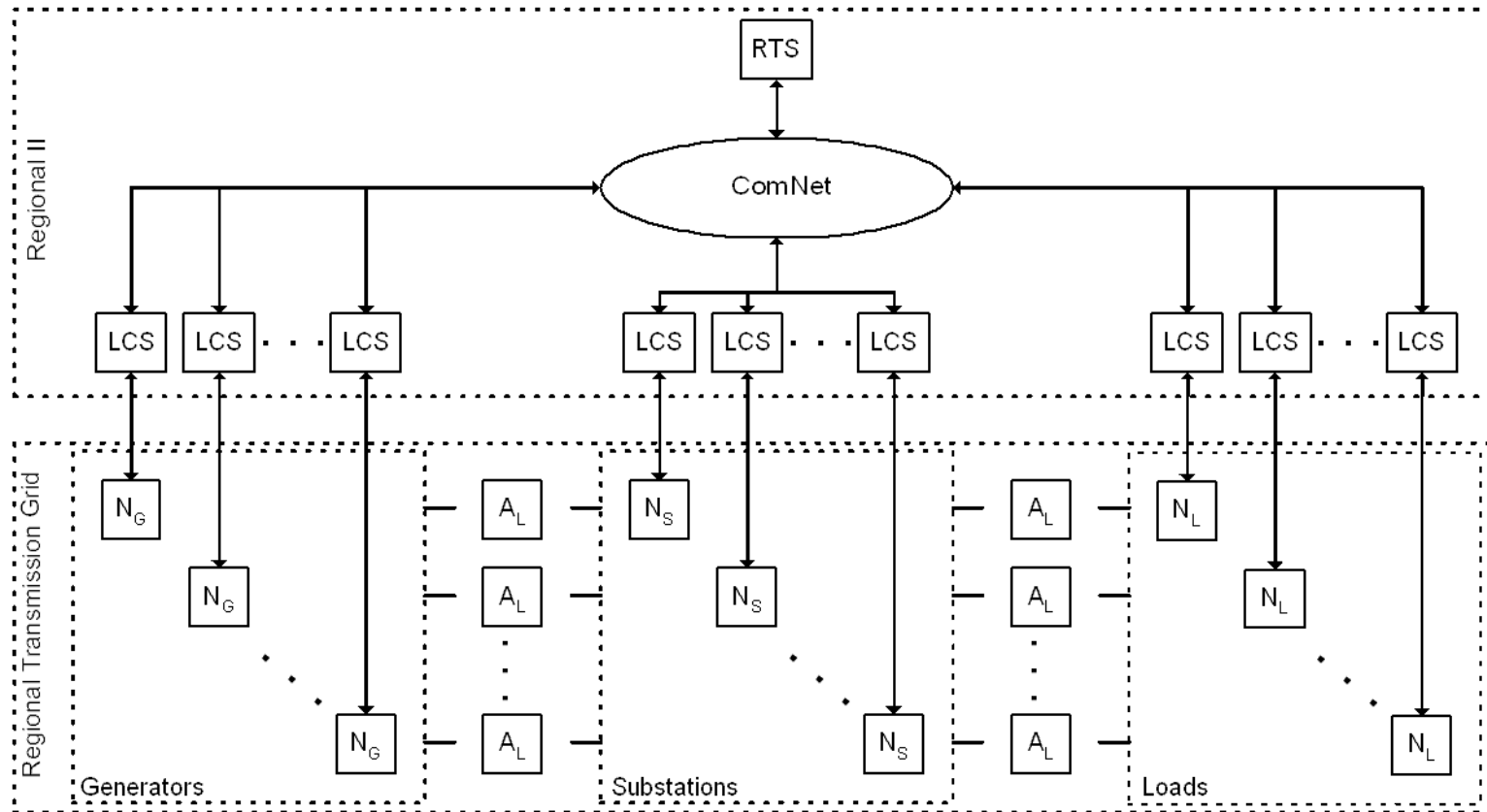
And accounting for

- Power overload and propagation
- EI components failures
- II components failures

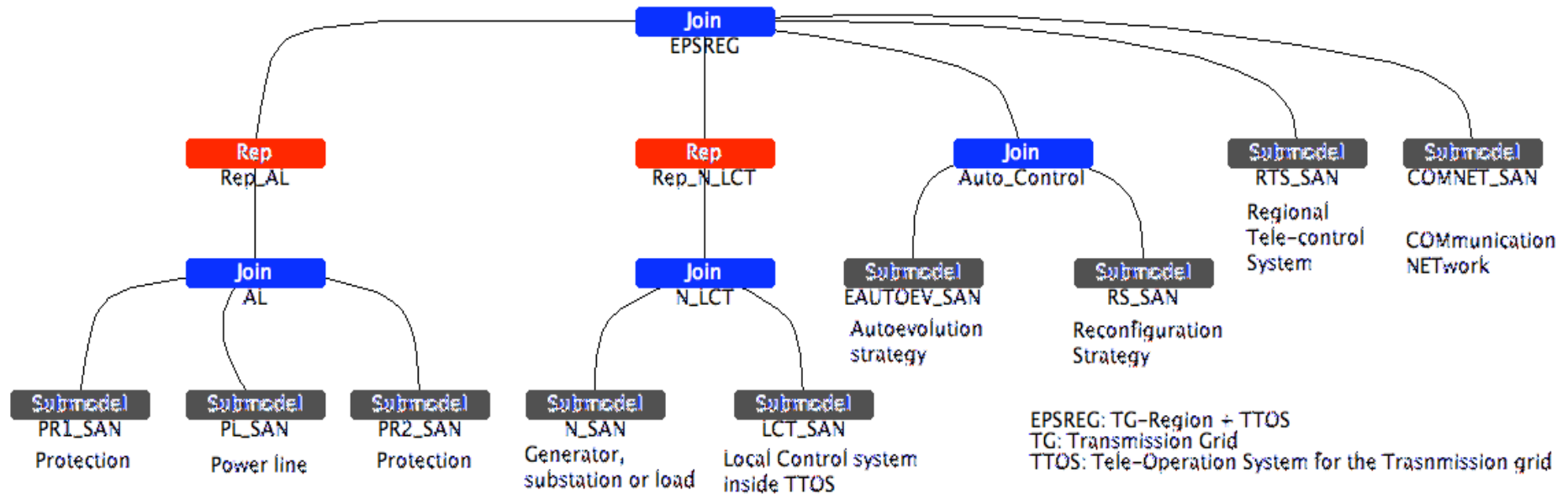
Major assumptions

- The EI state is determined by the equations for the DC power flow approximation (derived from the standard AC circuit equations), which give a **linear relationship** between:
 - the **power at the nodes** and
 - the **power flow on the lines**
- The definition of **RS₁()** and **RS₂()** depends on the policies and algorithms adopted by II. They are obtained by solving a **linear programming problem**
 - The new state determined by **RS₁()** is suboptimal wrt **RS₂()** (being based on local information);
 - **RS₁()** completes in time **T₁=0**, while **RS₂()** in time **T₂>0**

Logical structure of the analyzed EPS instance

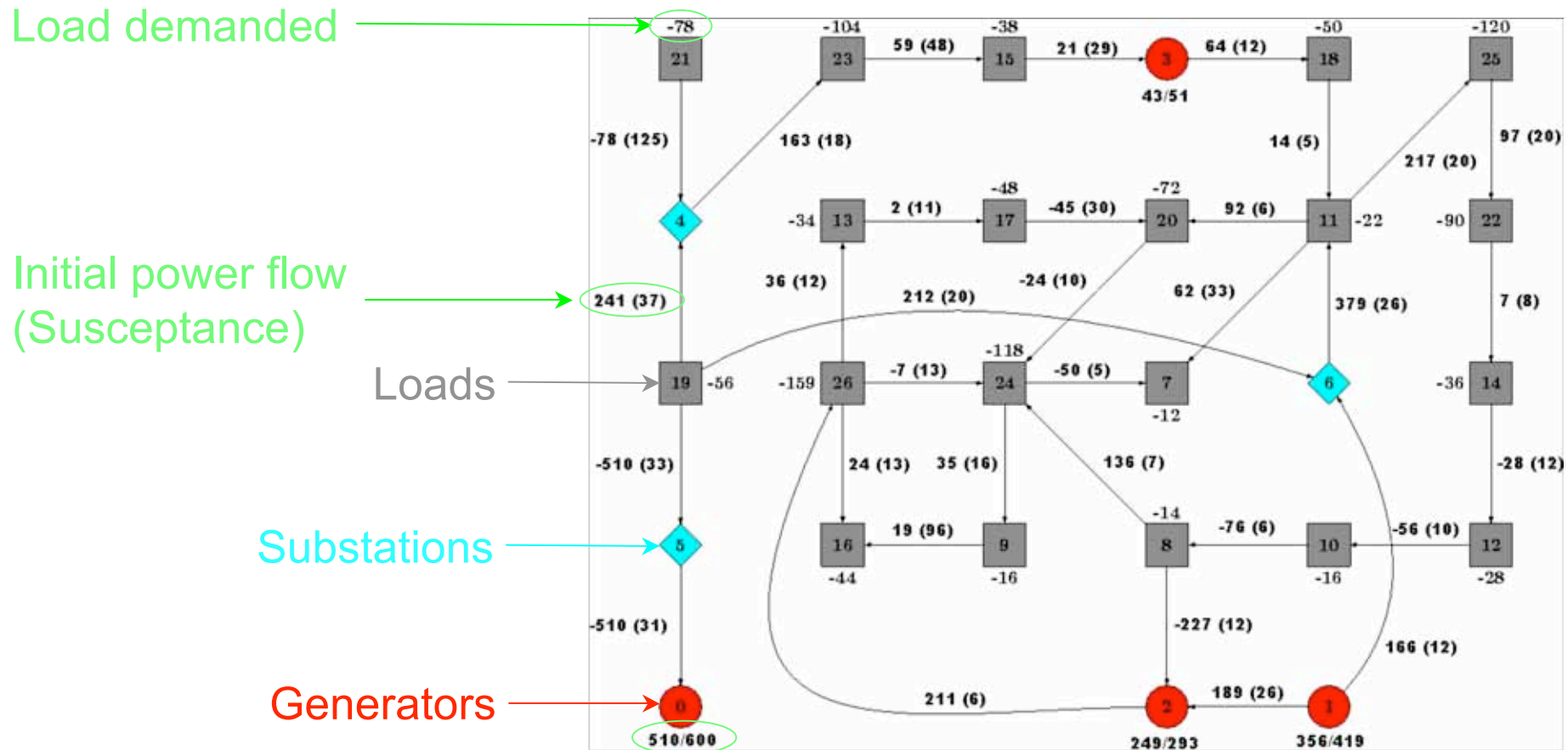


The Composed Model



- **Rep_AL**: nA not anonymous replicas of the model AL
- **Rep_N_LTC**: nN not anonymous replicas of the model N_LCT
- The submodels interact through common places

Diagram of the EI grid (a portion of the IEEE 118 Bus Test Case)



Maximum power flow through the lines = 620

Measure of interest

- $P_{UD}(t,t+1)$: *percentage of the mean power demand that is not met in the interval $[t,t+1]$ hours*
(the symbol 'UD' stands for 'Unsatisfied Demand').

It is a user-oriented measure of the blackout size and can be obtained as the load shed (i.e., the not served power due to a load shedding) divided by the power demand.

Analyzed scenario

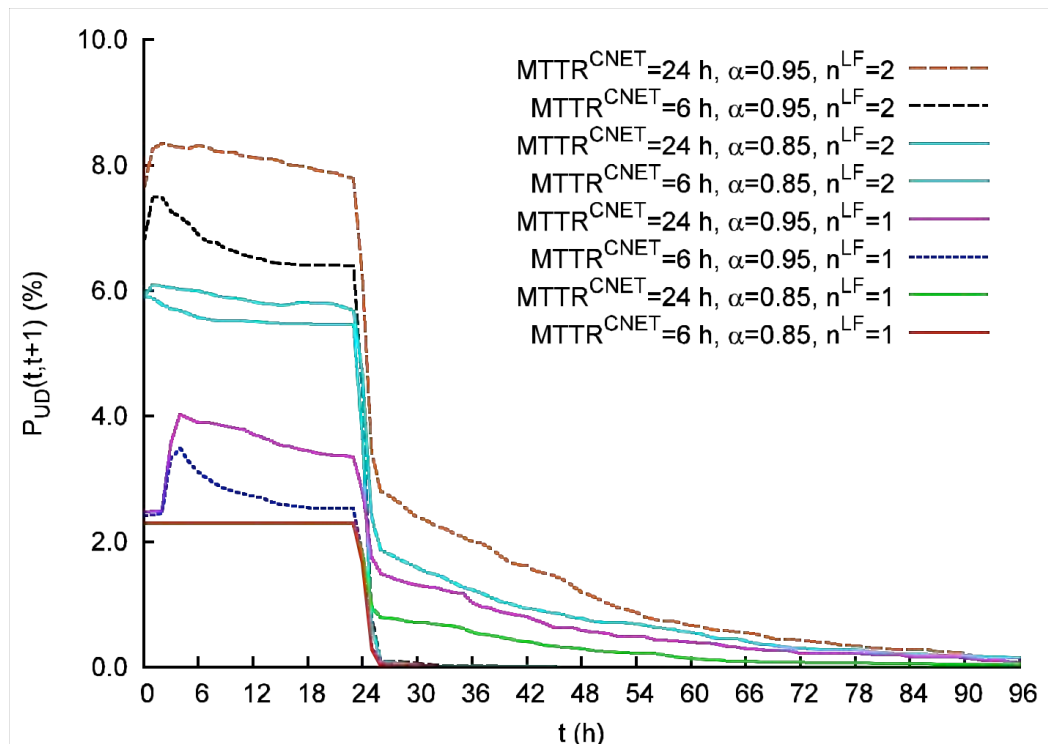
GOAL: assess the impact of the **omission failure of the communication network** (ComNet) on $P_{UD}(t,t+1)$ when a **simultaneous failure of a set of transmission lines** is occurred. More in detail:

- The grid starts in electrical equilibrium.
- At time zero, n^{LF} **power lines are simultaneously affected by a permanent failure** (e.g., due to a tree fall or a terrorist attack), thus becoming unavailable.
 - The power lines that fail are randomly (*uniformly*) selected from the set of all available power lines.
 - All the failed power lines are (*deterministically*) repaired after 24 hours.
- At the same time zero, **ComNet is simultaneously affected by a denial of service (DoS) attack**.
 - The DoS attack ends after an *exponentially* distributed time with mean $MTTR^{CNET}$, and from that time RTS can start computing the RTS reconfiguration action that will be (*deterministically*) applied after 10 minutes.

Sensitivity analysis campaign

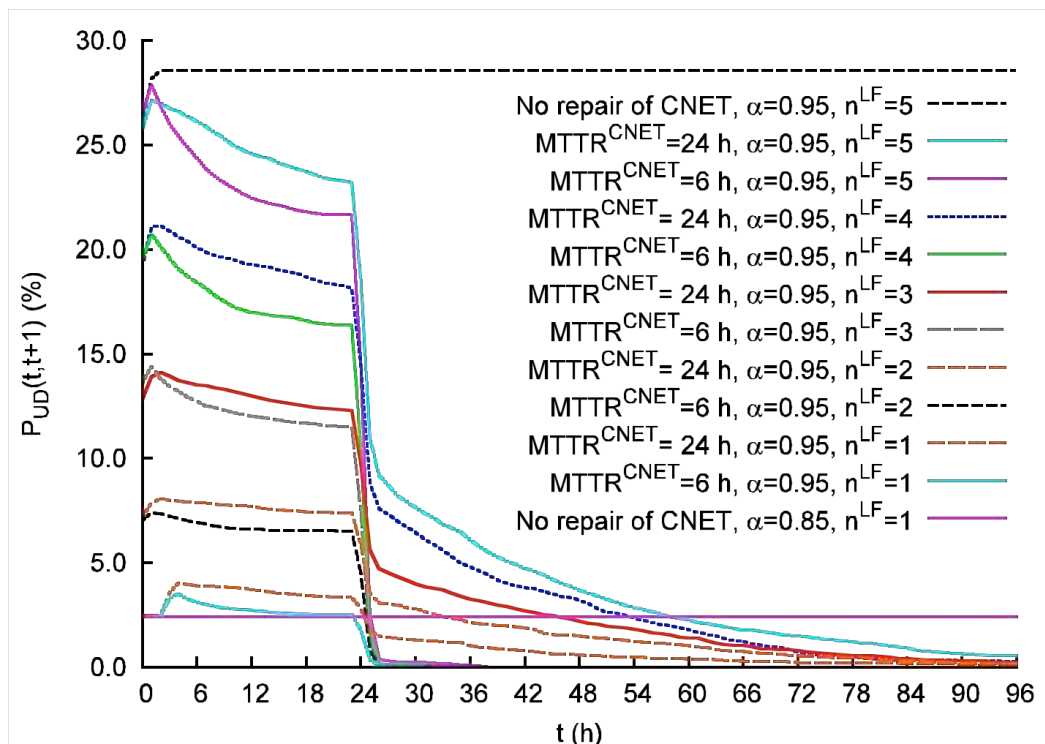
- A sensitivity analysis has been performed on the following parameters:
 - $MTTR^{CNET}$, thus **varying the duration of the DoS attack** affecting the communication network. If $MTTR^{CNET}$ goes to infinity, then we are modeling a RTS omission failure.
 - n^{LF} , thus **varying the severity of the overall EI failure**.
 - α , thus **varying the initial stress level of the power grid**.
 - ✓ For each generator i , α is defined as the ratio P_i/P_i^{max} .
 - ✓ In the initial grid setting all the ratios P_i/P_i^{max} are equal to a fixed value $\alpha=0.85$.

$P_{UD}(t,t+1)$, with $t=0,1,\dots,96$ h., for different values of $MTTR^{CNET}$ (6,24 h.), n^{LF} (1,2) and α (0.85,0.95)



- Unless for the lowest curves ($\alpha=0.85$, $n^{LF}=1$), the failure of even a single line at time zero produces an increment of $P_{UD}(t,t+1)$ until the reconfiguration is applied.
- At $t=24$ hours there is a big improvement (the failed power lines are repaired).
- The impact of the system stress level α is less heavy than the failure of power lines

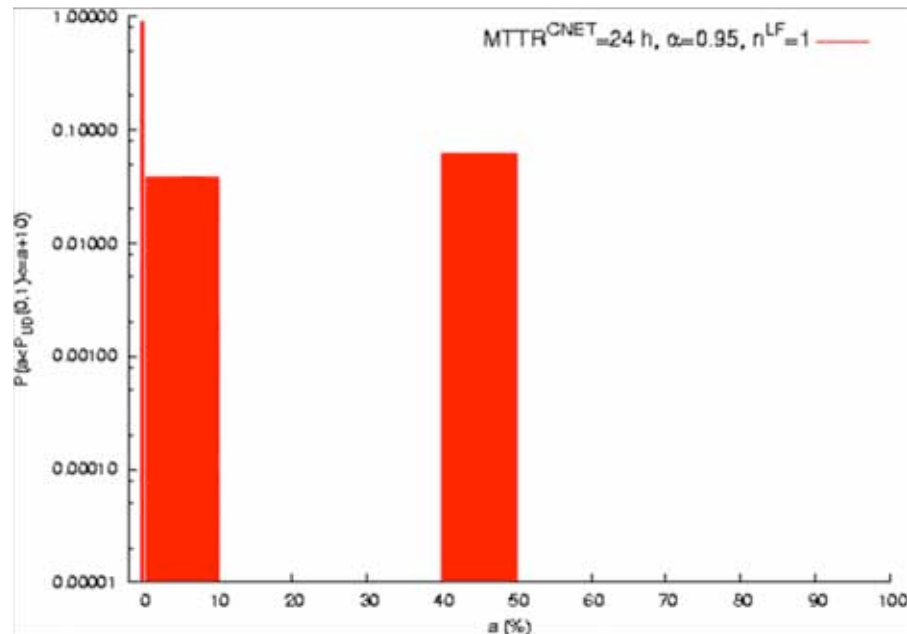
P_{UD}(t,t+1) ,with t=0,1,...,96 hours, for different values of MTTR^{CNET} (6,24 h.) and n^{LF} (1,...,5), fixing α=0.95



- P_{UD}(t,t+1) increases considering higher n^{LF} values, and fixing the value for n^{LF}, P_{UD}(t,t+1) gets worse in the case in which the DoS attack has a longer duration (24 hours).
- After 24 hours the disrupted power lines are repaired, and consequently P_{UD}(t,t+1) rapidly decreases until reaching the zero value.
- The top most curve represents the case of RTS omission failure

**Probability that $P_{UD}(0,1)$ is in the interval $(a,a+10]\%$,
with $a=0,10,\dots,90$,
fixing $\alpha=0.95$, $n^{LF}=1$ and $MTTR^{CNET}=24$ hours**

From the analysis of the previous figures, we know that $P_{UD}(0,1) \approx 2.5$.

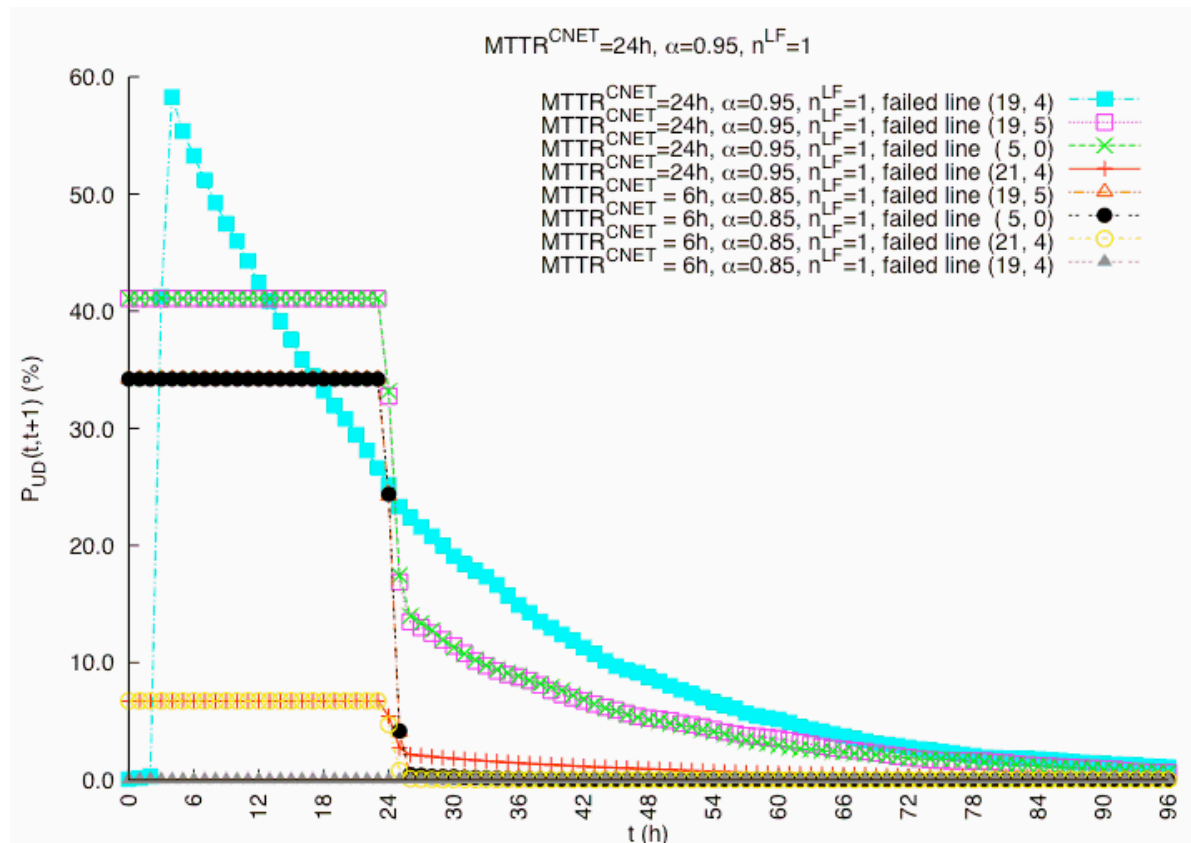


Analyzing its complete distribution we note that:

- with a very high probability the percentage of undelivered power is equal to zero;
- $P_{UD}(0,1)$ is in the interval $(0,10]\%$ with a probability of about 0.05, and it is in the interval $(40,50]\%$ with a probability of about 0.07;
- all the other probabilities are almost zero.

A mean loss of 40-50% of delivered power in the first hour of the system can happen, for example, when the power line affected by the failure is directly connected to a generator.

$P_{UD}(t,t+1)$ at varying the failed power line, with $t=0,1,\dots,96$ hours, for different values of $MTTR^{CNET}$ (6,24 h.) and α (0.95, 0.85)



- Only power lines for which $P_{UD}(t,t+1) > 0$ are displayed
- Allows to determine critical power lines

Ongoing and future work

- Detailed analysis and description of the EI grid's evolution through observing simulation runs
- Extension of the experimental campaign
 - by including the failures of other EI components
 - ✓ e.g., protections
 - by including other kinds of failures
 - ✓ e.g., lightning affecting power lines
 - by introducing other patterns of components failures
 - ✓ e.g., sequences of clusters of simultaneous failures
 - by enriching the set of measures of interest for the analyses
 - ✓ e.g., time to reach a certain black-out level
 - ✓ e.g., number of failed power lines/nodes in a certain interval of time